

Interfaces Java/Go

Typeclasses

C++ CONCERNS

Rust Traits
Scala

Overloading Operators: Arithmetic

The **+** operator works for a bunch of different types.

For Integer :

```
λ> 2 + 3
```

```
5
```

for Double precision floats:

```
λ> 2.9 + 3.5
```

```
6.4
```

Overloading Comparisons

Similarly we can *compare* different types of values

$\lambda > 2 == 3$

False

ea int
[Double]

$\lambda > [2.9, 3.5] == [2.9, 3.5]$

True

$\lambda > ("cat", 10) < ("cat", 2)$

False

ord (String, Int)

$\lambda > ("cat", 10) < ("cat", 20)$

True

"special case"

Ad-Hoc Overloading

Seems unremarkable?

*+
=
<
...*

*} make them
work on
MANY types*

Languages since the dawn of time have supported "operator overloading"

- To support this kind of **ad-hoc polymorphism**
- Ad-hoc: "created or done for a particular purpose as necessary."

You really need to *add* and *compare* values of *multiple* types!

Haskell has no caste system

No distinction between **operators** and **functions**

- All are first class citizens!

But then, what type do we give to *functions* like `+` and `==` ?

QUIZ

Which of the following would be appropriate types for `(+)` ?

- ~~(A)~~ `(+) :: Integer -> Integer -> Integer` } `2.3+4.1` would not check
- ~~(B)~~ `(+) :: Double -> Double -> Double` } `1+2` check
- ~~(C)~~ `(+) :: a -> a -> a` } `True+False`
- `(\x -> x) + (\z -> z+1)`

(D) *All of the above*

(E) *None of the above*

Integer -> Integer -> Integer is bad because?

- Then we cannot add Double s!

Double -> Double -> Double is bad because?

- Then we cannot add Double s!

$a \rightarrow a \rightarrow a$ is bad because?

- That doesn't make sense, e.g. to add two `Bool` or two `[Int]` or two functions!

Type Classes for Ad Hoc Polymorphism

Haskell solves this problem with **typeclasses**

- Introduced by Wadler and Blott (<http://portal.acm.org/citation.cfm?id=75283>)

How to make *ad-hoc* polymorphism less *ad hoc*

Philip Wadler and Stephen Blott
University of Glasgow*

October 1988

BTW: The paper is one of the clearest examples of academic writing I have seen. The next time you hear a curmudgeon say all the best CS was done in the 60s or 70s just point them to the above.

Qualified Types

To see the right type, lets ask:

$\lambda > \text{:type } (+)$

$(+) :: (\text{Num } a) \Rightarrow a \rightarrow a \rightarrow a$

We call the above a **qualified type**. Read it as +

- takes in two **a** values and returns an **a** value

for any type a that

- is a Num or
- *implements* the Num interface or }
- is an instance of a Num .

The name Num can be thought of as a *predicate* or *constraint* over types.

Some types are *Nums*

Examples include Integer , Double etc

- Any such values of those types can be passed to + .

Other types are not `Num`s

Examples include `Char` , `String` , functions etc,

- Values of those types *cannot* be passed to `+` .

```
λ> True + False
```

```
<interactive>:15:6:
```

```
  No instance for (Num Bool) arising from a use of +
```

```
  In the expression: True + False
```

```
  In an equation for ‘it’: it = True + False
```

Aha! Now those no **instance** for error messages should make sense!

- Haskell is complaining that `True` and `False` are of type `Bool`
- and that `Bool` is *not* an instance of `Num` .

Type Class is a Set of Operations

A typeclass is a collection of operations (functions) that must exist for the underlying type.

- Similar but different to Java interfaces (https://www.parsonsmatt.org/2017/01/07/how_do_type_classes_differ_from_interfaces.html)

Num a
(+)
(-)
from Integer ::

The **Eq** Type Class

The simplest typeclass is perhaps, Eq

```
class Eq a where  
  (==) :: a -> a -> Bool  
  (/=) :: a -> a -> Bool
```

A type `a` is an *instance of* `Eq` if there are two functions

- `==` and `/=`

That determine if two `a` values are respectively *equal* or *disequal*.

The Show Type Class

The typeclass `Show` requires that instances be convertible to `String` (which can then be printed out)

```
class Show a where  
  show :: a -> String
```

Indeed, we can test this on different (built-in) types

```
λ> show 2  
"2"
```

```
λ> show 3.14  
"3.14"
```

```
λ> show (1, "two", ([],[],[]))  
"(1,\"two\",([],[],[]))"
```

(Hey, whats up with the funny \" ?)

Unshowable Types

When we type an expression into `ghci`,

- it computes the value,
- then calls `show` on the result.

Thus, if we create a *new* type by

```
data Unshowable = A | B | C
```

and then create values of the type,

```
λ> let x = A
λ> :type x
x :: Unshowable
```

but then we **cannot view** them

```
λ> x
```

```
<interactive>:1:0:
```

```
  No instance for (Show Unshowable)
```

```
    arising from a use of `print` at <interactive>:1:0
```

```
  Possible fix: add an instance declaration for (Show Unshowabl
```

```
e)
```

```
  In a stmt of a 'do' expression: print it
```

and we **cannot compare** them!

```
λ> x == x
```

```
<interactive>:1:0:
```

```
  No instance for (Eq Unshowable)
```

```
    arising from a use of `==` at <interactive>:1:0-5
```

```
  Possible fix: add an instance declaration for (Eq Unshowable)
```

```
  In the expression: x == x
```

```
  In the definition of `it`: it = x == x
```

Again, the previously incomprehensible type error message should make sense to you.

Creating Instances

Tell Haskell how to show or compare values of type `Unshowable`

By **creating instances** of `Eq` and `Show` for that type:

```
instance Eq Unshowable where
```

```
  (==) A A = True           -- True if both inputs are A
```

```
  (==) B B = True           -- ...or B
```

```
  (==) C C = True           -- .. or C
```

```
  (==) _ _ = False         -- otherwise
```

```
  (/=) x y = not (x == y)  -- Test if `x == y` and negate result!
```

EXERCISE

Lets create an **instance** for `Show Unshowable`

When you are done we should get the following behavior

```
>>> x = [A, B, C]
[A, B, C]
```

Automatic Derivation

We *should* be able to compare and view `Unshowble` **automatically**"

Haskell lets us *automatically derive* implementations for some standard classes

```
data Showable = A' | B' | C'
  deriving (Eq, Show) -- tells Haskell to automatically generate i
  nstances
```

Now we have

```
λ> let x' = A'
```

```
λ> :type x'
```

```
x' :: Showable
```

```
λ> x'
```

```
A'
```

```
λ> x' == x'
```

```
True
```

```
λ> x' == B'
```

```
False
```

The Num typeclass

Let us now peruse the definition of the Num typeclass.

```
λ> :info Num
class (Eq a, Show a) => Num a where
  (+) :: a -> a -> a
  (*) :: a -> a -> a
  (-) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

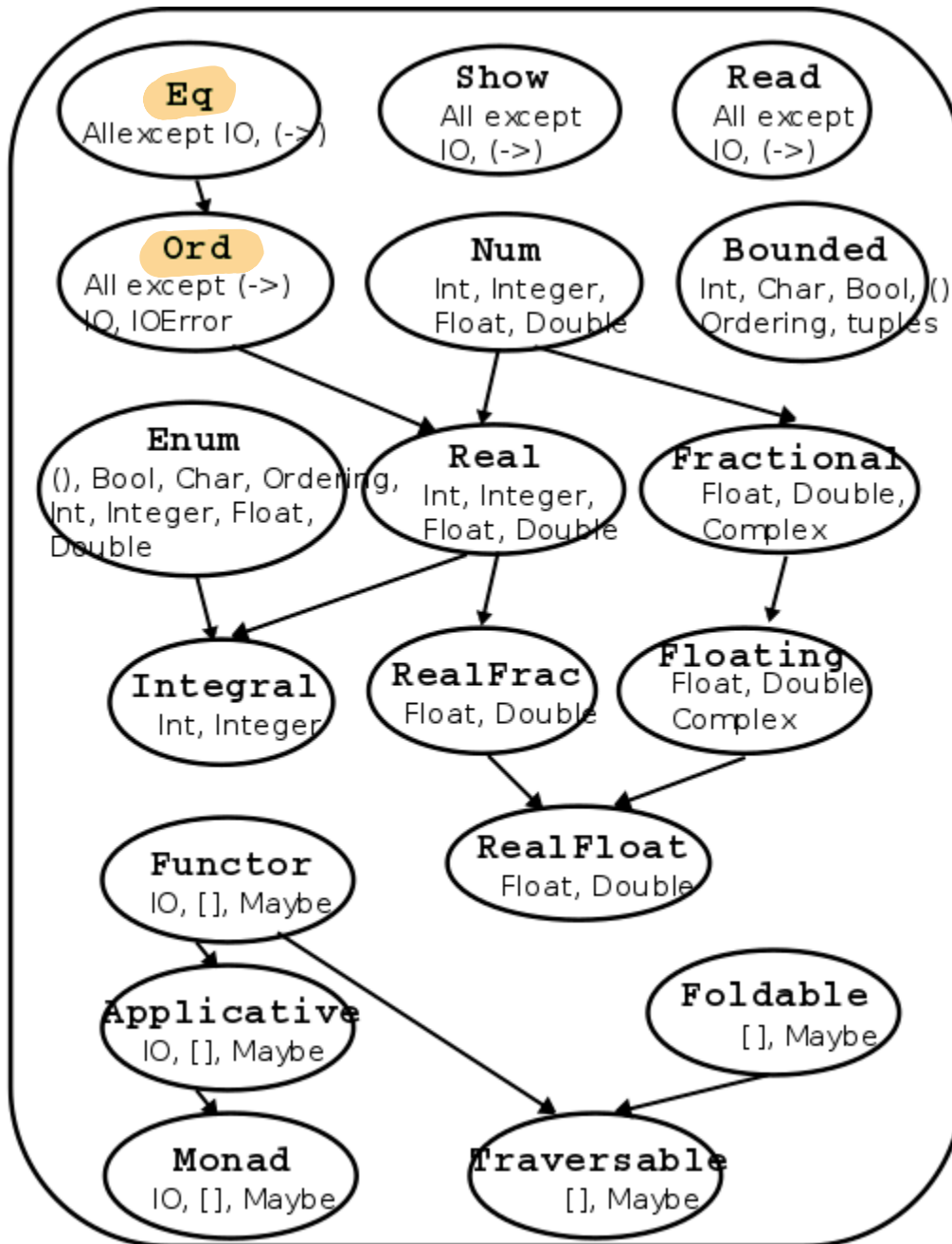
A type a is an instance of (i.e. implements) `Num` if

1. The type is *also* an instance of `Eq` and `Show`, and
2. There are functions to add, multiply, etc. values **of that type**.

That is, we can do *comparisons* and *arithmetic* on the values.

Standard Typeclass Hierarchy

Haskell comes equipped with a rich set of built-in classes.



Standard Typeclass Hierarchy

In the above picture, there is an edge from Eq and Show to Num because for something to be a Num it must also be an Eq and Show.

The *Ord* Typeclass

Another typeclass you've used already is the one for ordering values:

```
λ> :info (<)
```

```
class Eq a => Ord a where
```

```
...
```

```
(<) :: a -> a -> Bool
```

(≤)

```
...
```

For example:

```
λ> 2 < 3
```

```
True
```

```
λ> "cat" < "dog"
```

```
True
```

QUIZ

Recall the datatype:

```
data Showable = A' | B' | C' deriving (Eq, Show)
```

What is the result of:

```
λ> A' < B'
```

(A) True (B) False (C) Type error (D) Run-time exception

Using Typeclasses

Typeclasses integrate with the rest of Haskell's type system.

Lets build a small library for *Environments* mapping keys `k` to values `v`

```
data Table k v
  = Def v -- default value `v` to be used for "missing" keys
  | Bind k v (Table k v) -- bind key `k` to the value `v`
deriving (Show)
```

QUIZ

What is the type of keys

```
keys (Def _) = []  
keys (Bind k _ rest) = k : keys rest
```

- A. `Table k v -> k`
- B. `Table k v -> [k]`
- C. `Table k v -> [(k, v)]`
- D. `Table k v -> [v]`
- E. `Table k v -> v`

An API for Table

Lets write a small API for Table

```

-- >>> let env0 = set "cat" 10.0 (set "dog" 20.0 (Def 0))

-- >>> set "cat" env0
-- 10

-- >>> get "dog" env0
-- 20

-- >>> get "horse" env0
-- 0

```

Ok, lets implement!

```

-- | 'add key val env' returns a new env that additionally maps `k
  ey` to `val`
set :: k -> v -> Table k v -> Table k v
set key val env = ???

-- | 'get key env' returns the value of `key` and the "default" if
  no value is found
get :: k -> Table k v -> v
get key env = ???

```

Oops, y u no check?

Constraint Propagation

Lets *delete* the types of `set` and `get`

- to see what Haskell says their types are!

```
λ> :type get
```

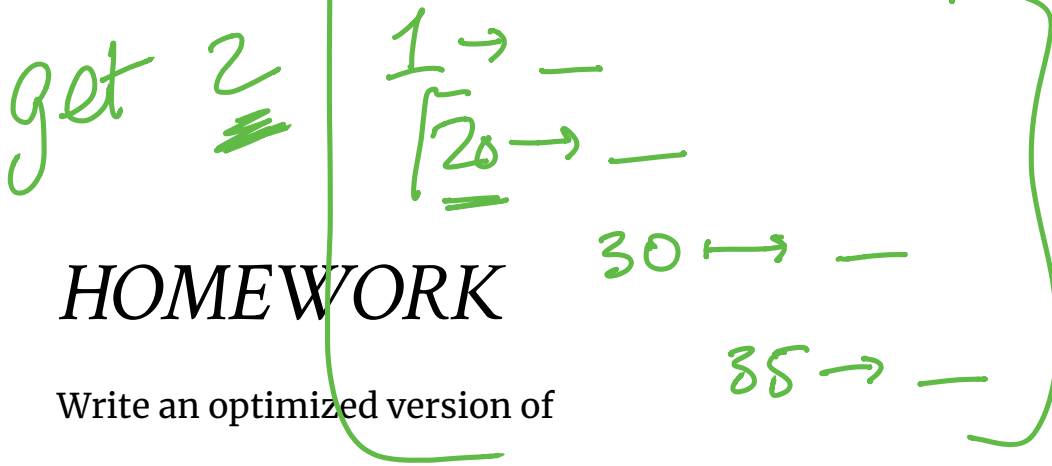
```
get :: (Eq k) => k -> v -> Table k v -> Table k v
```

We can use *any* `k` value as a *key* - if `k` is an instance of i.e. “implements” the `Eq` typeclass.

How, did GHC figure this out?

- If you look at the code for `get` you’ll see that we check if two keys *are equal*!





HOMEWORK

Write an optimized version of

- **set** that ensures the keys are in **increasing** order,
- **get** that **gives up** and returns the “default” the moment we see a **key that's larger than the one we're looking for.**
- (How) do you need to change the type of Table ?
- (How) do you need to change the types of get and set ?

Explicit Signatures

Sometimes the use of type classes requires explicit annotations

- which affect the code's behavior

Read is a standard typeclass that is the “opposite” of Show

- where any instance `a` of `Read` has a “parsing” function

```
read :: (Read a) => String -> a
```

QUIZ

What does the expression `read "2"` evaluate to?

- (A) compile time error
- (B) `"2" :: String`
- (C) `2 :: Integer`
- (D) `2.0 :: Double`
- (E) run-time exception

Compiler is puzzled!

Doesn't know *what type* to convert the string to!

Doesn't know *which* of the `read` functions to run!

- Did we want an `Int` or a `Double` or maybe something else altogether?

Explicit Type Annotation

- needed to tell Haskell what to convert the string to:

```
>>> (read "2") :: Int  
2
```

```
>>> (read "2") :: Float  
2.0
```

Note the different results due to the different types.

Creating Typeclasses

EQ, ORD, SHOW
NUM,

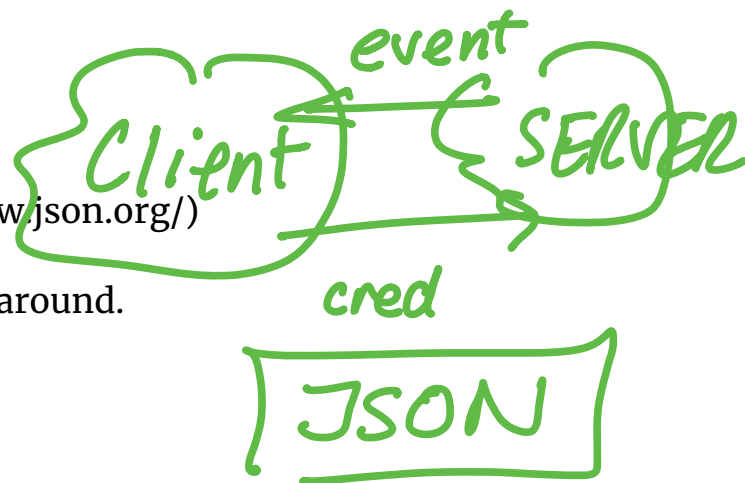
Typeclasses are useful for *many* different things.

We will see some of those over the next few lectures.

Lets conclude today's class with a quick example that provides a small taste.

JSON

Web-App



JavaScript Object Notation or JSON (<http://www.json.org/>)

- is a simple format for transferring data around.

Here is an example:

```

{ "name" : "Ranjit" ← STRING
  , "age" : 42.0 ← NUMBER
  , "likes" : ["guacamole", "coffee", "tacos"] ← ARRAY [STR]
  , "hates" : [ "waiting" , "spiders" ]
  , "lunches" : [ { "day" : "monday", "loc" : "zanzibar" }
                  , { "day" : "tuesday", "loc" : "farmers market" }
                  , { "day" : "wednesday", "loc" : "harekrishna" }
                  , { "day" : "thursday", "loc" : "faculty club" }
                  , { "day" : "friday", "loc" : "coffee cart" } ]
}

```

Handwritten annotations in green:

- Arrows pointing to "Ranjit", "42.0", and the array of likes.
- A large bracket on the left labeled "ARRAY" encompassing the "lunches" field.
- Underlines under "zanzibar", "farmers market", "harekrishna", "faculty club", and "coffee cart".

In brief, each JSON object is either

- a *base* value like a string, a number or a boolean,
- an (ordered) array of objects, or
- a set of *string-object* pairs. *key-val*

A JSON Datatype

We can represent (a subset of) JSON values with the Haskell datatype

```

data JVal
  = JStr  String
  | JNum  Double
  | JBool Bool
  | JObj  [(String, JVal)]
  | JArr  [JVal]
  deriving (Eq, Ord, Show)

```

Handwritten annotations in green:

- A large curly brace on the right side of the first three lines (JStr, JNum, JBool) is labeled "BASE".
- A curly brace on the right side of the JObj line is labeled "OBJ".
- A curly brace on the right side of the JArr line is labeled "ARRAY".

Thus, the above JSON value would be represented by the JVal

```

js1 :: JVal
js1 =
  JObj [ ("name", JStr "Ranjit")
        , ("age", JNum 41.0)
        , ("likes", JArr [ JStr "guacamole", JStr "coffee", JStr "
bacon" ])
        , ("hates", JArr [ JStr "waiting", JStr "grapefruit" ])
        , ("lunches", JArr [ JObj [ ("day", JStr "monday")
                                   , ("loc", JStr "zanzibar" )]
                              , JObj [ ("day", JStr "tuesday")
                                       , ("loc", JStr "farmers market" )]
                              , JObj [ ("day", JStr "wednesday")
                                       , ("loc", JStr "hare krishna" )]
                              , JObj [ ("day", JStr "thursday")
                                       , ("loc", JStr "faculty club" )]
                              , JObj [ ("day", JStr "friday")
                                       , ("loc", JStr "coffee cart" )]
                              ]
        ]

```

Ordinary
Haskell



JVal

Int, Bool, String, Map Int String

Serializing Haskell Values to JSON

Lets write a small library to *serialize* Haskell values as JSON.

We could write a bunch of functions like

```
doubleToJSON :: Double -> JVal  
doubleToJSON = JNum
```

```
stringToJSON :: String -> JVal  
stringToJSON = JStr
```

```
boolToJSON   :: Bool -> JVal  
boolToJSON   = JBool
```

Serializing Collections

But what about collections, namely *lists* of things?

```
doublesToJSON    :: [Double] -> JVal  
doublesToJSON xs = JArr (map doubleToJSON xs)
```

```
boolsToJSON      :: [Bool] -> JVal  
boolsToJSON xs  = JArr (map boolToJSON xs)
```

```
stringsToJSON    :: [String] -> JVal  
stringsToJSON xs = JArr (map stringToJSON xs)
```

This is getting rather tedious

- We are rewriting the same code :(

Serializing Collections (refactored with HOFs)

You could abstract by making the *individual-element-converter* a parameter

```
xsToJSON :: (a -> JVal) -> [a] -> JVal
```

```
xsToJSON f xs = JArr (map f xs)
```

```
xysToJSON :: (a -> JVal) -> [(String, a)] -> JVal
```

```
xysToJSON f kvs = JObject (map (\(k, v) -> (k, f v)) kvs)
```

Serializing Collections Still Tedious

As we have to specify the individual data converter (yuck!)

```
λ> doubleToJSON 4
```

```
JNum 4.0
```

```
λ> xsToJSON stringToJSON ["coffee", "guacamole", "bacon"]
```

```
JArr [JStr "coffee", JStr "guacamole", JStr "bacon"]
```

```
λ> xysToJSON stringToJSON [("day", "monday"), ("loc", "zanzibar")]
```

```
JObj [("day", JStr "monday"), ("loc", JStr "zanzibar")]
```

This gets *awful* when you have richer objects like

```
lunches = [ [("day", "monday"), ("loc", "zanzibar")
             , [("day", "tuesday"), ("loc", "farmers market")]
           ]
```

because we have to go through gymnastics like


```
λ> xsToJSON (xysToJSON stringToJSON) lunches
JArr [ JObject [{"day",JStr "monday"} ,{"loc",JStr "zanzibar"}]
      , JObject [{"day",JStr "tuesday"} ,{"loc",JStr "farmers marke
t"}]
      ]
```

Yikes. So much for *readability*

Is it too much to ask for a magical `toJSON` that *just works*?

Typeclasses To The Rescue

Lets *define* a typeclass that describes types `a` that can be converted to JSON.

```
class JSON a where
  toJSON :: a -> JVal
```

Now, just make all the above instances of `JSON` like so

```
instance JSON Double where
```

```
  toJSON = JNum
```

```
instance JSON Bool where
```

```
  toJSON = JBool
```

```
instance JSON String where
```

```
  toJSON = JStr
```

This lets us uniformly write

```
λ> toJSON 4
```

```
JNum 4.0
```

```
λ> toJSON True
```

```
JBool True
```

```
λ> toJSON "guacamole"
```

```
JStr "guacamole"
```

Bootstrapping Instances

Haskell can *automatically bootstrap* the above to *lists* and *tables*!

```
instance JSON a => JSON [a] where  
  toJSON xs = JArr (map toJSON xs)
```

- if `a` is an instance of `JSON`,
- then here's how to convert *lists* of `a` to `JSON`.

```
λ> toJSON [True, False, True]  
JArr [JBln True, JBln False, JBln True]
```

```
λ> toJSON ["cat", "dog", "Mouse"]  
JArr [JStr "cat", JStr "dog", JStr "Mouse"]
```

Bootstrapping Lists of Lists!

```
λ> toJSONN [["cat", "dog"], ["mouse", "rabbit"]]
JArr [JArr [JStr "cat",JStr "dog"],JArr [JStr "mouse",JStr "rabbit"]]
```

Bootstrapping Key-Value Tables

We can pull the same trick with key-value lists

```
instance (JSON a) => JSON [(String, a)] where
  toJSONN kvs = JObject (map \(k, v) -> (k, toJSONN v)) kvs)
```

after which, we are all set!

```
λ> toJSONN lunches
JArr [ JObject [ ("day",JStr "monday"), ("loc",JStr "zanzibar") ]
      , JObject [ ("day",JStr "tuesday"), ("loc",JStr "farmers market") ]
      ]
```

Bootstrapping Tuples

Lets bootstrap the serialization for tuples (upto some fixed size)

```
instance (JSON a, JSON b) => JSON ((String, a), (String, b)) where  
  toJSON ((k1, v1), (k2, v2)) = JObject  
    [ (k1, toJSON v1)  
      , (k2, toJSON v2)  
    ]
```

```
instance (JSON a, JSON b, JSON c) => JSON ((String, a), (String,  
b), (String, c)) where  
  toJSON ((k1, v1), (k2, v2), (k3, v3)) = JObject  
    [ (k1, toJSON v1)  
      , (k2, toJSON v2)  
      , (k3, toJSON v3)  
    ]
```

```
instance (JSON a, JSON b, JSON c, JSON d) => JSON ((String, a), (S  
tring, b), (String, c), (String,d)) where  
  toJSON ((k1, v1), (k2, v2), (k3, v3), (k4, v4)) = JObject  
    [ (k1, toJSON v1)  
      , (k2, toJSON v2)  
      , (k3, toJSON v3)  
      , (k4, toJSON v4)  
    ]
```

```
instance (JSON a, JSON b, JSON c, JSON d, JSON e) => JSON ((Strin  
g, a), (String, b), (String, c), (String,d), (String, e)) where  
  toJSON ((k1, v1), (k2, v2), (k3, v3), (k4, v4), (k5, v5)) = JObject  
    [ (k1, toJSON v1)  
      , (k2, toJSON v2)  
      , (k3, toJSON v3)  
      , (k4, toJSON v4)  
      , (k5, toJSON v5)  
    ]
```

Now, we can simply write

```
hs = (("name"    , "Ranjit")
      ,("age"    , 41.0)
      ,("likes"  , ["guacamole", "coffee", "bacon"])
      ,("hates"  , ["waiting", "grapefruit"])
      ,("lunches", lunches)
      )
```

which is a Haskell value that describes our running JSON example, and can convert it directly like so

```
js2 = toJSON hs
```

EXERCISE: Serializing Tables

To wrap everything up, lets write a routine to serialize our Table

```
instance JSON (Table k v) where
  toJSON env = ???
```

and presto! our serializer *just works*

```
>>> env0
Bind "cat" 10.0 (Bind "dog" 20.0 (Def 0))

>>> toJSON env0
JObj [ ("cat", JNum 10.0)
      , ("dog", JNum 20.0)
      , ("def", JNum 0.0)
      ]
```

Thats it for today.

We will see much more typeclass awesomeness in the next few lectures...

(<https://ucsd-cse230.github.io/sp20/feed.xml>) (<https://twitter.com/ranjitjhala>)
(<https://plus.google.com/u/0/104385825850161331469>)
(<https://github.com/ranjitjhala>)

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